

Tests for Symmetry

There are three types of symmetry: symmetric with respect to the y-axis, symmetric with respect to the x-axis, and symmetric with respect to the origin.

1. If (x, y) is a point on the graph and $(-x, y)$ is also a point on the graph, the portion of the graph to the left of the y-axis is a *mirror image* of the portion to the right of the y-axis.
2. If (x, y) is a point on the graph and $(x, -y)$ is also a point on the graph, the portion of the graph above the x-axis is a *mirror image* of the portion below the x-axis.
3. If (x, y) is a point on the graph and $(-x, -y)$ is also a point on the graph, the graph is *unchanged* by a rotation of 180° about the origin.

Find the axis of symmetry for the following problems:

$$y = x^2 - 6$$

$$y^2 = x^3 - 8x$$

$$xy = 4$$

$(-x, y)$ Symmetric about the y-axis	$(x, -y)$ Symmetric about the x-axis	$(-x, -y)$ Symmetric about the origin
$y = x^2 - 6$	$y = x^2 - 6$	$y = x^2 - 6$
$y = (-x)^2 - 6$	$-y = x^2 - 6$	$-y = (-x)^2 - 6$
$y = x^2 - 6$	$-y = x^2 - 6$	$-y = x^2 - 6$
$y^2 = x^3 - 8x$	$y^2 = x^3 - 8x$	$y^2 = x^3 - 8x$
$y^2 = (-x)^3 - 8(-x)$	$(-y)^2 = x^3 - 8x$	$(-y)^2 = (-x)^3 - 8(-x)$
$y^2 = -x^3 + 8x$	$y^2 = x^3 - 8x$	$y^2 = -x^3 + 8x$
$xy = 4$	$xy = 4$	$xy = 4$
$(-x)y = 4$	$x - y = 4$	$(-x)(-y) = 4$
$-xy = 4$	$-xy = 4$	$xy = 4$

After substituting in the negatives and solving, the final equation should equal the beginning equation. This provides you with the axis of symmetry.